

# Lecture 2: Metrics and Measurement

17-313: Foundations of Software Engineering  
Fall 2023

# Administrivia

- Slack
  - Add profile picture (if you want).
  - Ask questions in #general or #project-one. Use threads.
- Homework 1 is released. It is due Wed Aug 30, 11:59 pm (one week!)
  - This is an individual assignment
  - Get started early, ask for help, and check the #project-one channel; chances are decent your questions have been asked by others! Office hours are running
- Complete the team formation survey today!
- Reading for next Sunday will be posted on the website
  - Gradescope quiz due before class.

# Learning Goals



Use measurements as a decision tool to reduce uncertainty



Understand difficulty of measurement; discuss validity of measurements



Provide examples of metrics for software qualities and process



Understand limitations and dangers of decisions and incentives based on measurements

Software Engineering: Principles, practices (technical and non-technical) for **confidently** building **high-quality** software.

What does this mean?  
How do we know?  
→ *Measurement* and metrics are **key** concerns.

# Outline

- Case Study: AV Vehicles
- Definitions: Measurements and Metrics
  - Examples: Code Complexity
  - Measurement scales
- Why measure?
- Risks and challenges
- Measures and incentives

# Case study: Autonomous Vehicles

# AV Software is \_\_\_\_\_



# How can we judge AV software quality (e.g. safety)?



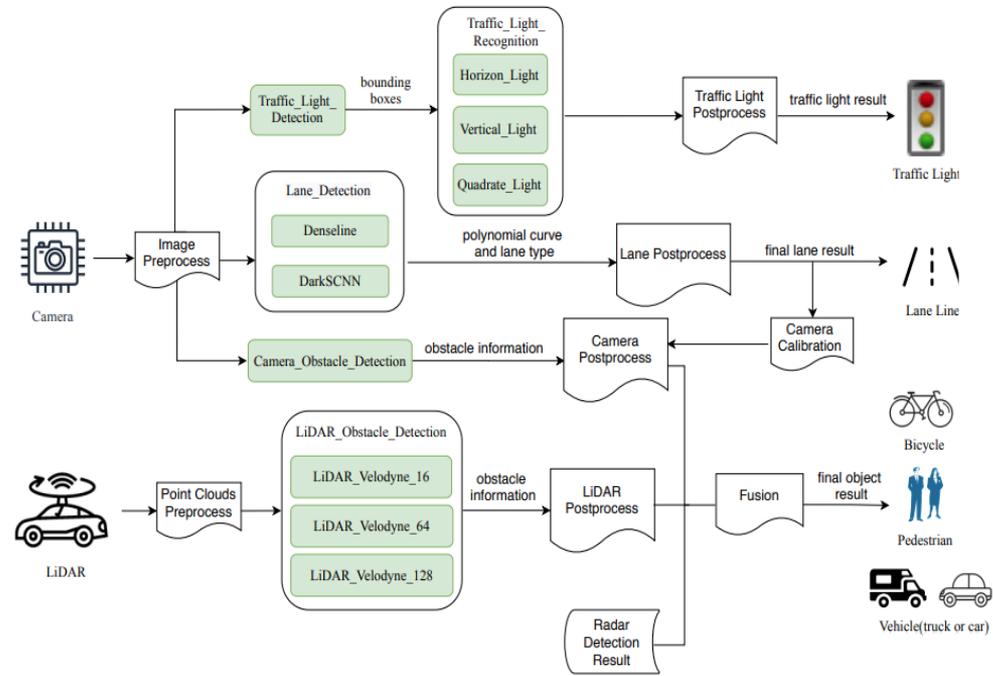
# Test coverage

- Amount of code executed during testing.
- Statement coverage, line coverage, branch coverage, etc.
- E.g., 75% branch coverage → 3/4 if-else outcomes have been executed

```
:
: 1698 : const TrajectoryPoint& StGraphData::init_point() const { return init_point; }
:
: 2264 : const SpeedLimit& StGraphData::speed_limit() const { return speed_limit; }
:
: 212736 : double StGraphData::cruise_speed() const {
[- +] 212736 :     return cruise_speed_ > 0.0 ? cruise_speed_ : FLAGS_default_cruise_speed;
: }
:
: 1698 : double StGraphData::path_length() const { return path_data_length; }
:
: 1698 : double StGraphData::total_time_by_conf() const { return total_time_by_conf; }
:
: 1698 : planning_internal::STGraphDebug* StGraphData::mutable_st_graph_debug() {
: 1698 :     return st_graph_debug;
: }
:
: 566 : bool StGraphData::SetSTDrivableBoundary(
:     const std::vector<std::tuple<double, double, double>&& s_boundary,
:     const std::vector<std::tuple<double, double, double>&& v_obs_info) {
[ + -] 566 :     if (s_boundary.size() != v_obs_info.size()) {
:         return false;
:     }
[ + +] 40752 :     for (size_t i = 0; i < s_boundary.size(); ++i) {
: 80372 :         auto st_bound_instance = st_drivable_boundary_.add_st_boundary();
: 160744 :         st_bound_instance->set_t(std::get<0>(s_boundary[i]));
: 120558 :         st_bound_instance->set_s_lower(std::get<1>(s_boundary[i]));
: 120558 :         st_bound_instance->set_s_upper(std::get<2>(s_boundary[i]));
[- +] 40186 :         if (std::get<1>(v_obs_info[i]) > -kObsSpeedIgnoreThreshold) {
: 0 :             st_bound_instance->set_v_obs_lower(std::get<1>(v_obs_info[i]));
:         }
[ + +] 40186 :         if (std::get<2>(v_obs_info[i]) < kObsSpeedIgnoreThreshold) {
: 50254 :             st_bound_instance->set_v_obs_upper(std::get<2>(v_obs_info[i]));
:         }
:     }
: }
```

# Model Accuracy

- Train machine-learning models on labelled data (sensor data + ground truth).
- Compute accuracy on a separate labelled test set.
- E.g., 90% accuracy implies that object recognition is right for 90% of the test inputs.



Source: Peng et al. ESEC/FSE'20

# Failure Rate

- Frequency of crashes/fatalities
- Per 1000 rides, per million miles, per month (in the news)

TRANSP / WAYMO / TECH

## Waymo's driverless cars were involved in two crashes and 18 'minor contact events' over 1 million miles



Image: Allen J. Schaben / Los Angeles Times via Getty Images

/ The Alphabet-owned company pulls back the curtain on more stats from its public road testing. Of the 20 incidents, only two met the federal government's reporting criteria, and no one was injured.

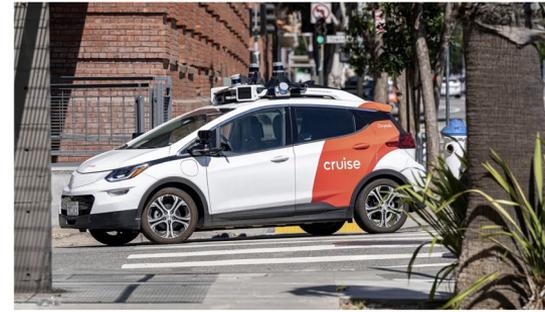
By [Andrew J. Hawkins](#), transportation editor with 10+ years of experience who covers EVs, public transportation, and aviation. His work has appeared in *The New York Daily News* and *City & State*.

Feb 28, 2023, 8:00 PM GMT+3 | [1 Comment](#) / [1 New](#)



## 'Complete meltdown': Driverless cars in San Francisco stall causing a traffic jam

By [Jordan Valinsky](#), CNN Business  
Updated 3:45 PM EDT, Mon August 14, 2023



A Cruise autonomous taxi in San Francisco.

# Mileage

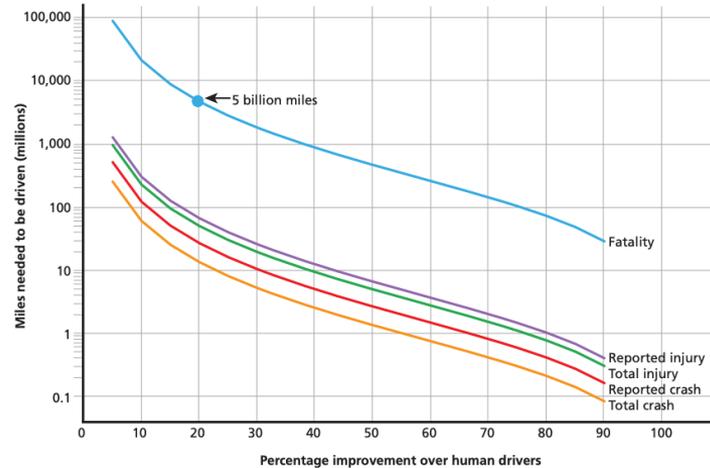


## Driving to Safety

How Many Miles of Driving Would It Take to Demonstrate Autonomous Vehicle Reliability?

Nidhi Kalra, Susan M. Paddock

Figure 3. Miles Needed to Demonstrate with 95% Confidence that the Autonomous Vehicle Failure Rate Is Lower than the Human Driver Failure Rate



# Building the World's Most Experienced Driver™

The Waymo Driver gains experience with every mile, in each car. ↘



10+

More than a Decade of Autonomous Driving in More than 10 States

5

Generations of Autonomously Driven Vehicles

15+

Billion Autonomously Driven Miles in Simulation

20+

Million Real-World Miles on Public Roads

Source: waymo.com/safety (September 2021)

# Activity

Think of “pros” and “cons” for using various metrics to judge AV software.

|                  |                              |
|------------------|------------------------------|
| Test coverage    | Age of codebase              |
| Model accuracy   | Time of most recent change   |
| Failure rate     | Frequency of code releases   |
| Size of codebase | Amount of code documentation |
| Mileage          | Number of contributors       |

- Group discussion, 5 minutes
- Write down two pros and two cons for three metrics on a piece of paper
- Write down your Andrew IDs.
- Keep the paper. You must hand in the paper at the end of the lecture.

# Outline

- Case Study: AV Vehicles
- **Definitions: Measurements and Metrics**
  - Examples: Code Complexity
  - Measurement scales
- Why measure?
- Risks and challenges
- Measures and incentives

# MEASUREMENT AND METRICS

# What is Measurement?

- **Measurement is the empirical, objective assignment of numbers, according to a rule derived from a model or theory, to attributes of objects or events with the intent of describing them.** – Craner, Bond, “Software Engineering Metrics: What Do They Measure and How Do We Know?”
- **A quantitatively expressed reduction of uncertainty based on one or more observations.** – Hubbard, “How to Measure Anything ...”

# Software Quality Metrics

- IEEE 1061 definition: **“A software quality metric is a function whose inputs are software data and whose output is a single numerical value that can be interpreted as the degree to which the software possesses a given attribute that affects its quality.”**
- Metrics have been proposed for many quality attributes; may define own metrics

# What software qualities do we care about? (examples)

- Scalability
- Security
- Extensibility
- Documentation
- Performance
- Consistency
- Portability
- Installability
- Maintainability
- Functionality (e.g., data integrity)
- Availability
- Ease of use

# What process qualities do we care about? (examples)

- On-time release
- Development speed
- Meeting efficiency
- Conformance to processes
- Time spent on rework
- Reliability of predictions
- Fairness in decision making
- Measure time, costs, actions, resources, and quality of work packages; compare with predictions
- Use information from issue trackers, communication networks, team structures, etc...

# Everything is measurable

- If X is something we care about, then X, by definition, must be detectable.
  - How could we care about things like “quality,” “risk,” “security,” or “public image” if these things were totally undetectable, directly or indirectly?
  - If we have reason to care about some unknown quantity, it is because we think it corresponds to desirable or undesirable results in some way.
- If X is detectable, then it must be detectable in some amount.
  - If you can observe a thing at all, you can observe more of it or less of it
- If we can observe it in some amount, then it must be measurable.

Douglas Hubbard, How to Measure Anything, 2010

# EXAMPLES: CODE COMPLEXITY

# Lines of Code

- Easy to measure

```
> wc -l file1 file2...
```

| LOC           | projects             |
|---------------|----------------------|
| 450           | Expression Evaluator |
| 2,000         | Sudoku               |
| 100,000       | Apache Maven         |
| 500,000       | Git                  |
| 3,000,000     | MySQL                |
| 15,000,000    | gcc                  |
| 50,000,000    | Windows 10           |
| 2,000,000,000 | Google (MonoRepo)    |

# Normalizing Lines of Code

- Ignore comments and empty lines
- Ignore lines < 2 characters
- Pretty print source code first
- Count statements (logical lines of code)
- See also: cloc

```
for (i = 0; i < 100; i += 1) printf("hello"); /* How many lines of code is this? */
```

```
/* How many lines of code is this? */  
  
for (  
    i = 0;  
    i < 100;  
    i += 1  
){  
    printf("hello");  
}
```

# Normalization per Language

| Language  | Statement factor<br>(productivity) | Line factor |
|-----------|------------------------------------|-------------|
| C         | 1                                  | 1           |
| C++       | 2.5                                | 1           |
| Fortran   | 2                                  | 0.8         |
| Java      | 2.5                                | 1.5         |
| Perl      | 6                                  | 6           |
| Smalltalk | 6                                  | 6.25        |
| Python    | 6                                  | 6.5         |

Source: "Code Complete: A Practical Handbook of Software Construction", S. McConnell, Microsoft Press (2004)  
and <http://www.codinghorror.com/blog/2005/08/are-all-programming-languages-the-same.html> u.a.

# Halstead Volume

- Introduced by Maurice Howard Halstead in 1977
- Halstead Volume =  
    number of operators/operands \*  
     $\log_2(\text{number of distinct operators/operands})$
- Approximates size of elements and vocabulary

# Halstead Volume - Example

- ```
main() {  
    int a, b, c, avg;  
    scanf("%d %d %d", &a, &b, &c);  
    avg = (a + b + c) / 3;  
    printf("avg = %d", avg);  
}
```

Operators/Operands: main, (), {}, int, a, b, c, avg, scanf, (), "...", &, a, &, b, &, c, avg, =, a, +, b, +, c, (), /, 3, printf, (), "...", avg

# Cyclomatic Complexity

- Proposed by McCabe 1976
- Based on control flow graph, measures linearly independent paths through a program
  - $\approx$  number of decisions
  - Number of test cases needed to achieve branch coverage

```
if (c1) {  
    f1();  
} else {  
    f2();  
}  
if (c2) {  
    f3();  
} else {  
    f4();  
}
```

$M = \text{edges of CFG} - \text{nodes of CFG} + 2 * \text{connected components}$

*"For each module, either limit cyclomatic complexity to [X] or provide a written explanation of why the limit was exceeded."*  
– NIST Structured Testing methodology

# Object-Oriented Metrics

- Number of Methods per Class
- Depth of Inheritance Tree
- Number of Child Classes
- Coupling between Object Classes
- Calls to Methods in Unrelated Classes
- ...

# Measurement scales

# Measurement scales: why they are important

- Scale: the type of data being measured.
- **The scale dictates what sorts of analysis/arithmetic is legitimate or meaningful.**
- Your options are:
  - Nominal: categories
  - Ordinal: order, but no magnitude.
  - Interval: order, magnitude, but no zero.
  - Ratio: Order, magnitude, and zero.

# Measurement scales: what you can do

01

## NOMINAL

Named variables

## ORDINAL

Named + ordered variables

02

03

## INTERVAL

Named + ordered + proportionate interval between variables

## RATIO

Named + ordered + proportionate interval between variables  
+ Can accommodate absolute zero

04

| Provides:                                      | Nominal | Ordinal | Interval | Ratio |
|------------------------------------------------|---------|---------|----------|-------|
| The "order" of values is known                 |         | ✓       | ✓        | ✓     |
| "Counts," aka "Frequency of Distribution"      | ✓       | ✓       | ✓        | ✓     |
| Mode                                           | ✓       | ✓       | ✓        | ✓     |
| Median                                         |         | ✓       | ✓        | ✓     |
| Mean                                           |         |         | ✓        | ✓     |
| Can quantify the difference between each value |         |         | ✓        | ✓     |
| Can add or subtract values                     |         |         | ✓        | ✓     |
| Can multiple and divide values                 |         |         |          | ✓     |
| Has "true zero"                                |         |         |          | ✓     |

# Outline

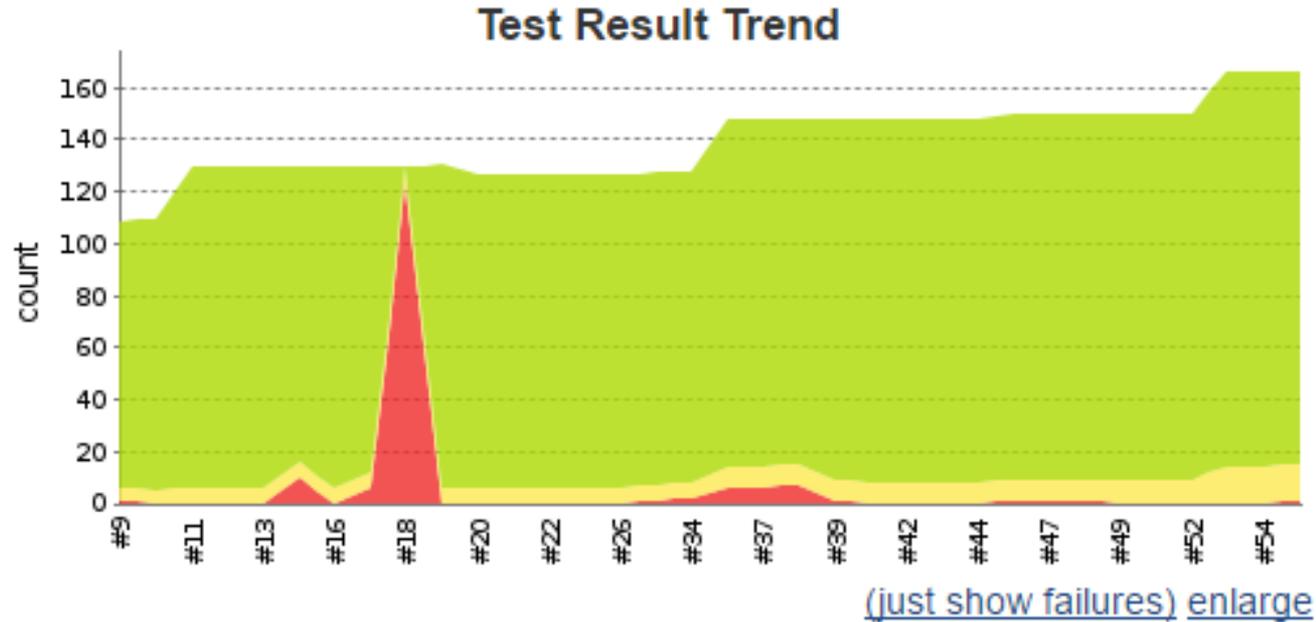
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# WHY MEASURE?

# Measurement for Decision Making

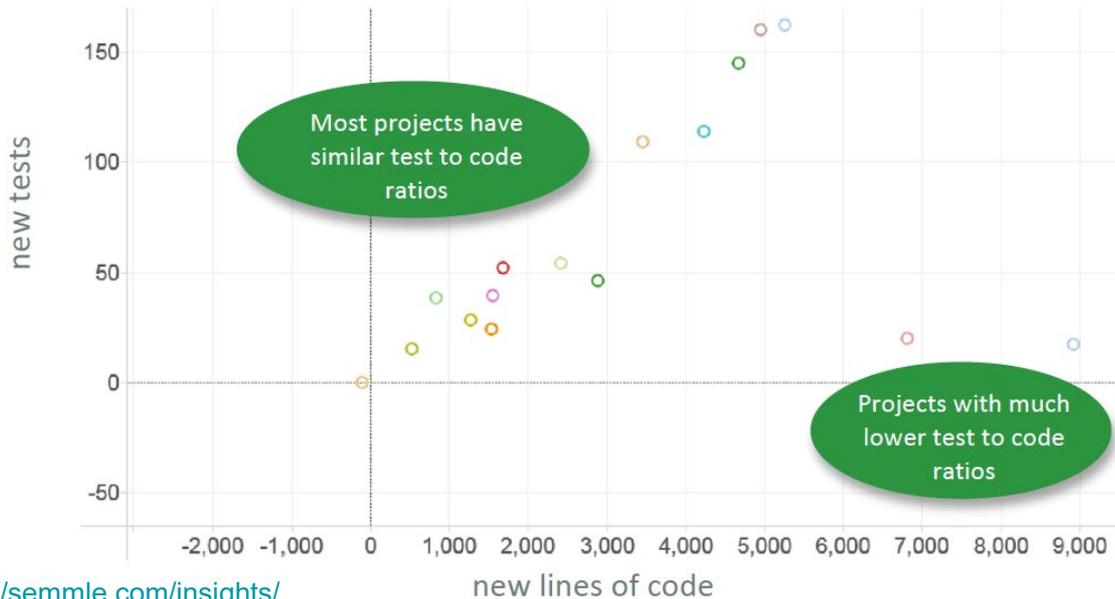
- Fund project?
- More testing?
- Fast enough? Secure enough?
- Code quality sufficient?
- Which feature to focus on?
- Developer bonus?
- Time and cost estimation? Predictions reliable?

# Trend analyses



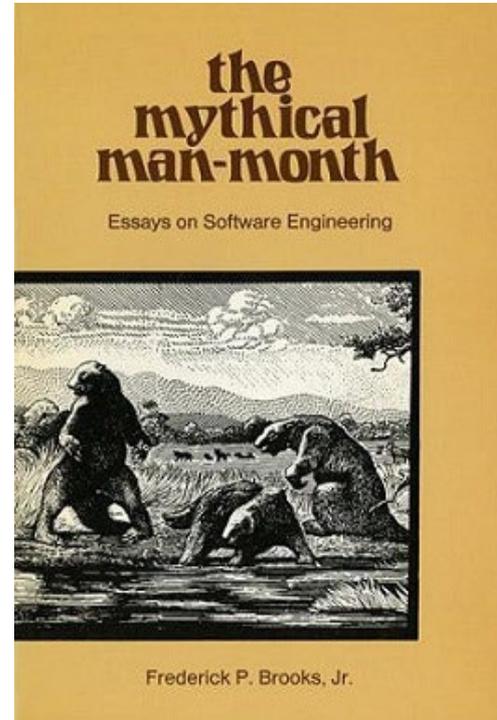
# Benchmarking against standards

- Monitor many projects or many modules, get typical values for metrics
- Report deviations



# Antipatterns in effort estimation

- IBM in the 60's: Would account in "person-months"  
e.g. Team of 2 working 3 months = 6 person-months
- LoC ~ Person-months ~ \$\$\$
- Brooks: *"Adding manpower to a late software project makes it later."*



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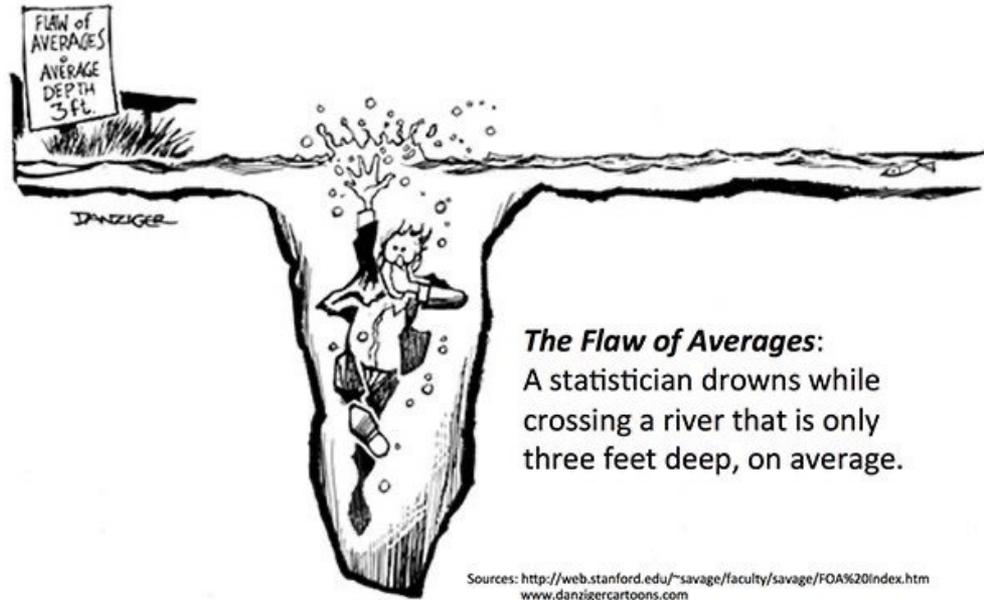
# The streetlight effect



- A known observational bias.
- People tend to look for something only where it's easiest to do so.
  - If you drop your keys at night, you'll tend to look for it under streetlights.

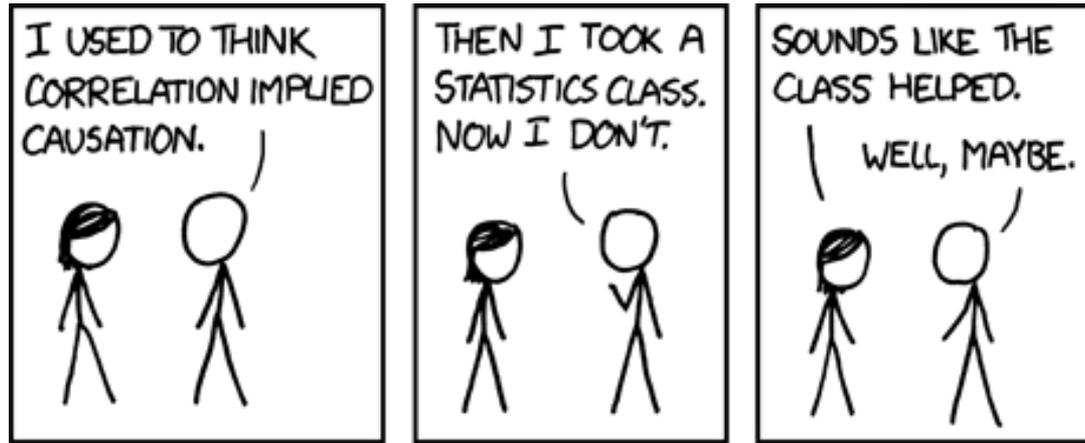
# Bad metrics: What could possibly go wrong?

- Bad statistics: A basic misunderstanding of measurement theory and what is being measured.
- Bad decisions: The incorrect use of measurement data, leading to unintended side effects.
- Bad incentives: Disregard for the human factors, or how the cultural change of taking measurements will affect people.



# Making inferences

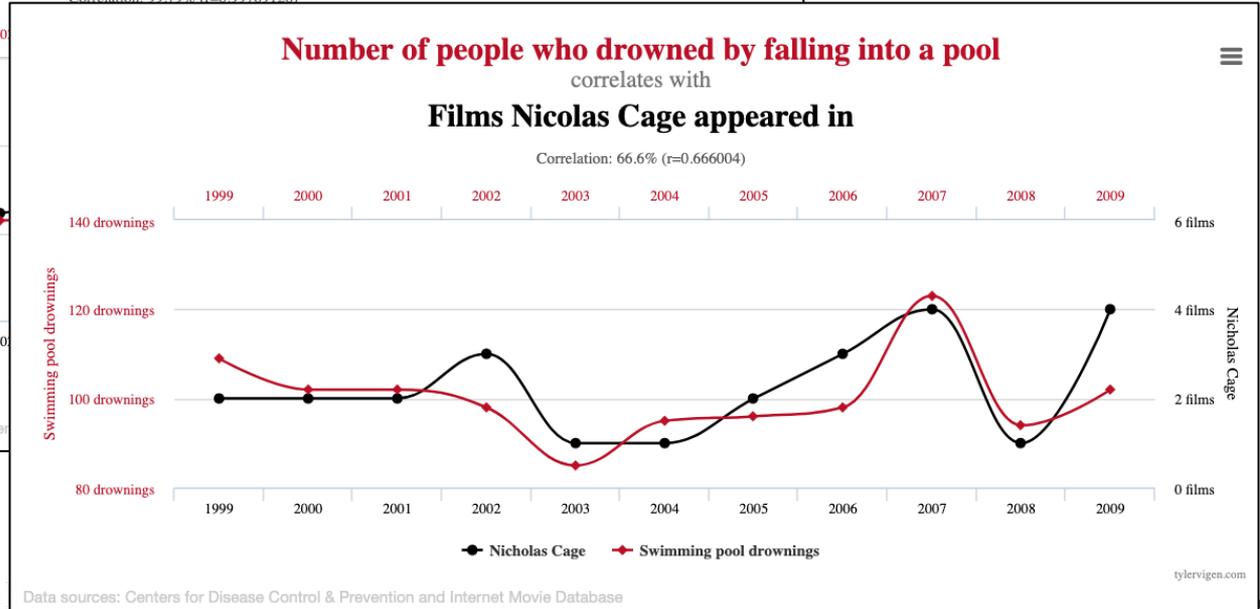
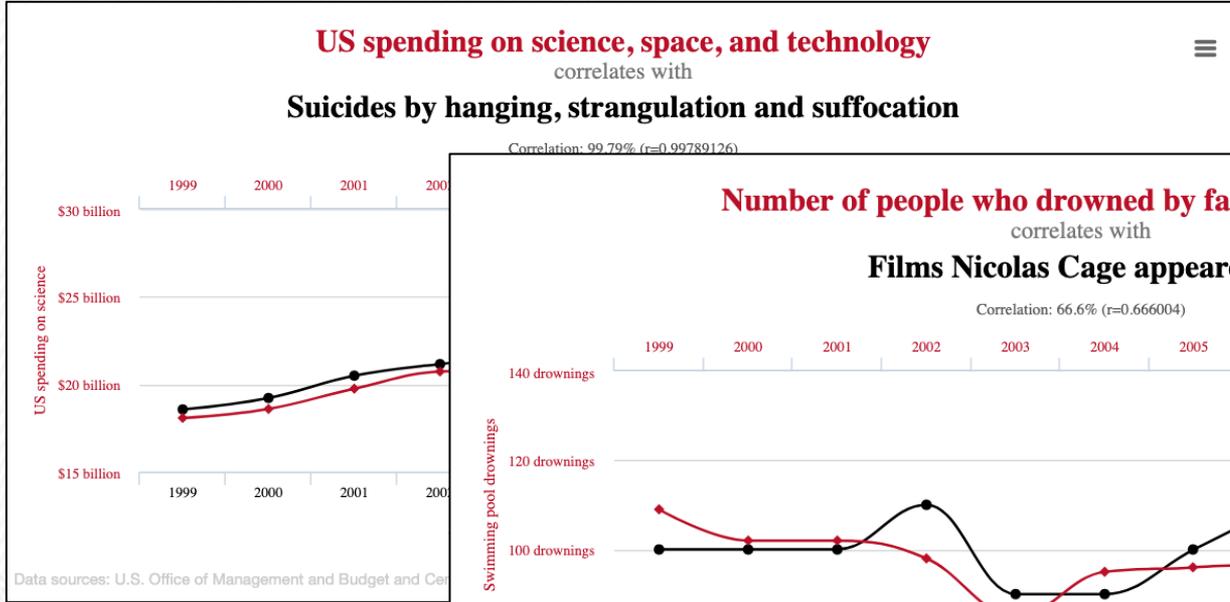
<http://xkcd.com/552/>



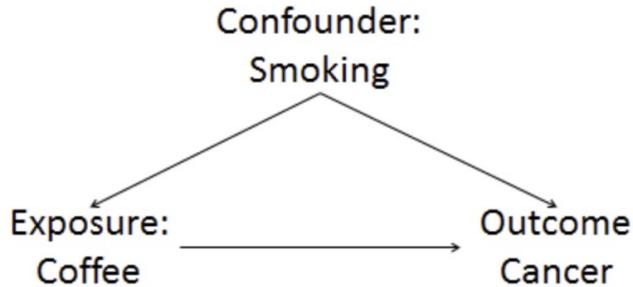
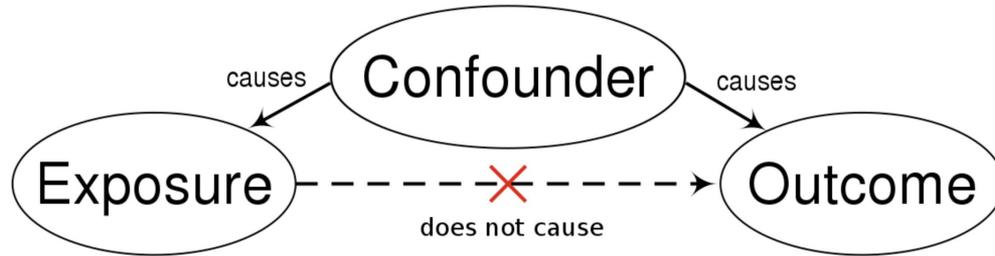
To infer causation:

- Provide a theory (from domain knowledge, independent of data)
- Show correlation
- Demonstrate ability to predict new cases (replicate/validate)

# Spurious Correlations



# Confounding variables



- If you look only at the coffee consumption → cancer relationship, you can get very misleading results
- Smoking is a confounder

“We found that there is a low to moderate correlation between coverage and effectiveness when the number of test cases in the suite is controlled for.”

RESEARCH-ARTICLE

## Coverage is not strongly correlated with test suite effectiveness

Authors:  [Laura Inozemtseva](#),  [Reid Holmes](#) [Authors Info & Affiliations](#)

ICSE 2014: Proceedings of the 36th International Conference on Software Engineering • May 2014 • Pages 435–445 • <https://doi.org/10.1145/2568225.2568271>

Most studies did not account for the confounding influence of test suite size

# Measurements validity

- *Construct validity* – Are we measuring what we intended to measure?
- *Internal validity* – The extent to which the measurement can be used to explain some other characteristic of the entity being measured
- *External validity* – Concerns the generalization of the findings to contexts and environments, other than the one studied

# Measurements reliability

- Extent to which a measurement yields similar results when applied multiple times
- Goal is to reduce uncertainty, increase consistency
- Example: Performance
  - Time, memory usage
  - Cache misses, I/O operations, instruction execution count, etc.
- Law of large numbers
  - Taking multiple measurements to reduce error
  - Trade-off with cost



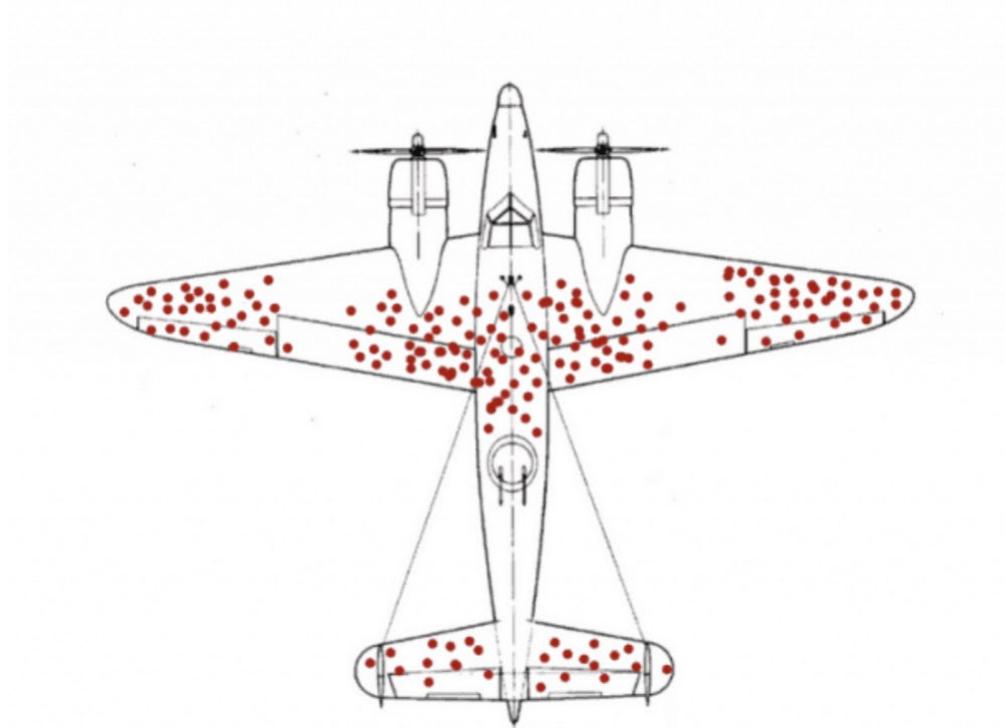
# McNamara fallacy

- Measure whatever can be easily measured.
- Disregard that which cannot be measured easily.
- Presume that which cannot be measured easily is not important.
- Presume that which cannot be measured easily does not exist.



<https://chronotopeblog.com/2015/04/04/the-mcnamara-fallacy-and-the-problem-with-numbers-in-education/> in University

# Survivorship bias



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# Goodhart's law: "When a measure becomes a target, it ceases to be a good measure."



<http://dilbert.com/strips/comic/1995-11-13/>

## *The Price of Wells Fargo's Fake Account Scandal Grows by \$3 Billion*

The bank reached a settlement with federal prosecutors and the Securities and Exchange Commission after abusing customers.

 Share full article



 199



Wells Fargo used fraud to open up fake accounts and force customers into services

# Productivity Metrics

- Lines of code per day?
  - Industry average 10-50 lines/day
  - Debugging + rework ca. 50% of time
- Function/object/application points per month
- Bugs fixed?
- Milestones reached?

# Incentivizing Productivity

- What happens when developer bonuses are based on
  - Lines of code per day?
  - Amount of documentation written?
  - Low number of reported bugs in their code?
  - Low number of open bugs in their code?
  - High number of fixed bugs?
  - Accuracy of time estimates?

# Summary

- Measurement is difficult but important for decision making
- Software metrics are easy to measure but hard to interpret, validity often not established
- Many metrics exist, often composed; pick or design suitable metrics if needed
- Careful in use: monitoring vs incentives
- Strategies beyond metrics

# What you need to know



Use measurements as a decision tool to reduce uncertainty



Understand difficulty of measurement; discuss validity of measurements



Provide examples of metrics for software qualities and process



Understand limitations and dangers of decisions and incentives based on measurements

# Questions to consider (HW1)

- What properties do we care about, and how do we measure it?
- What is being measured? Does it (to what degree) capture the thing you care about? What are its limitations?
- How should it be incorporated into process?
- What are potentially negative side effects or incentives?